Algebra Qualifying Exam Fall 2015 3 hours

- 1. Classify groups of order 55 up to isomorphism. Give a presentation for each of the groups in your classi cation.
- 2. Let R = C[X; Y] and consider the ideal I = (X; Y) as an R-module.
 - (a) Construct an exact sequence oR-modules

- (b) Prove that the sequence you constructed is not split.
- 3. Consider the ideal

$$I = (X^2 Y; Y^2 X) C[X; Y]$$
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Find all maximal ideals of the quotient C[X; Y]=I. (Find means give a set of generators.)

- 4. How many Sylow p-subgroups are there in $Gl_2(F_D)$?
- 5. SupposeK is an extension ofQ of degreen, and let $_1; :::; _n : K ! C$ be the distinct embeddings ofK into C. Let $_2$ K